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Spatially resolved, substrate-induced rectification in C₆₀ bilayers on copper

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We demonstrate rectification ratios (*RR*) of $\gtrsim 1000$ at biases of 1.3 V in bilayers of C₆₀ deposited on copper. Using scanning tunneling spectroscopy and first-principles calculations, we show that the strong coupling between C₆₀ and the Cu(111) surface leads to the metallization of the bottom C₆₀ layer, while the molecular orbitals of the top C₆₀ are essentially unaffected. Due to this substrate-induced symmetry breaking and to a tunneling transport mechanism, the system behaves as a hole-blocking layer, with a spatial dependence of the onset voltage on intra-layer coordination. Together with previous observations of strong electron-blocking character of pentacene/C₆₀ bilayers on Cu(111), this work further demonstrates the potential of strongly hybridized, C₆₀-coated electrodes to harness the electrical functionality of molecular components. *Published by AIP Publishing*. [http://dx.doi.org/10.1063/1.4975795]

I. INTRODUCTION

Going beyond the use of molecules as merely resistive elements is central to creating higher electrical functionality in organic optoelectronics devices. The earliest proposal for such non-linear electrical behavior is the Aviram-Ratner molecular diode model, proposed in 1974.¹ Following theoretical models of large rectification,^{2,3} much experimental work has been done in optimizing the intrinsic molecular properties, level alignment, and electronic coupling to electrodes.^{4–13} While rectification ratios in excess of 100 have been reported for ionically¹¹ or electrostatically gated¹³ molecules, the electrical performance of such molecular devices remains several orders of magnitude below that of their inorganic counterparts. A primary reason is that, despite their high tunability, molecules are very sensitive to their immediate environment, so that much of their desirable intrinsic electrical properties are lost when integrated into actual devices due to the spectral broadening of the molecular levels. Minimizing such effects leads to an apparent paradox, as it implies the physical decoupling of the electrodes from the active region of the device, which dramatically degrades its electrical performance.

In a previous work,¹⁴ we showed this paradox can be entirely overcome by using metallized molecules¹⁵ as a buffer layer between the active device region and the metallic electrode. Specifically, the strong coupling between C_{60} and the (111) surface of Cu leads to good electron and hole injection from the metal (due to a strongly broadened density of states around the Femi energy), while limiting interactions between the metal and molecules deposited in a second layer. In Ref. 14, using a donor pentacene monolayer on top of $C_{60}/Cu(111)$, we synthesized electron-blocking layers with average rectification ratios in excess of 1000 at 1 V, where the current flow is suppressed for a positively biased sample.

In this work, we demonstrate large rectification ratios in bilayers of C_{60} deposited on copper, where the symmetry

between the layers is broken by the strong $C_{60}/Cu(111)$ interaction. Using scanning tunneling microscopy and spectroscopy (STM/STS), we show that dense, close-packed second layers of C₆₀ form on top of C₆₀/Cu(111) and exhibit large rectification ratios. Using density functional theory (DFT), we show that—while the bottom layer of C_{60} is metallized—the second layer conserves its original accepting and semiconducting character, leading to rectification. Interestingly, in contrast to pentacene/ C_{60} /Cu(111), the system is a hole-blocking layer (i.e., current flow is suppressed for a negatively biased sample), showing the versatility and the potential of the $C_{60}/Cu(111)$ system to support non-linear current-voltage characteristics. Additionally, spatially resolved I(V) curves reveal a shift in the "on" voltage of the rectifier between the edge and the "bulk" of the bilayer; this phenomenon is reproduced in the calculations and explained as a Stark effect dependent on the local intra-layer coordination.

II. METHODS

Measurements were carried out in an ultrahigh-vacuum (UHV) variable-temperature (VT) STM operating with the sample maintained at 60 K. The Cu(111) crystal was cleaned by sputtering with Ar⁺ ions at 1 keV and simultaneously annealing at 900 K, with a final sputtering cycle at room temperature followed by a brief anneal at 900 K. C₆₀ was deposited on the same UHV system using an organic molecular-beam evaporator at 710 K. This C₆₀ film was annealed to \approx 570 K, either during deposition or immediately after. This process results in the desorption of any C₆₀ molecules not in immediate contact with the Cu substrate. It also causes Cu atoms to diffuse away from locations beneath C₆₀ molecules¹⁶ These Cu atoms relocate to nearby step edges, where they tend to attach in such a way as to straighten step edges along

close-packed rows, resulting in facetted crystallographic steps. The 2-d structure of the film is $p(4 \times 4)$. The second C₆₀ layer was deposited in the same way but with the sample at room temperature.

Tungsten tips were prepared by electrochemical etching; when they occasionally adsorbed molecules during experiments, they were cleaned by *in situ* UHV heating to approximately 1000 K to restore imaging and spectroscopic quality. Bias voltage V_B was applied to the sample. The I(V) curves were obtained with a "grid" spectroscopy approach, where the measurements were obtained sequentially in a grid pattern over the relevant region of the sample. Due to our high sensitivity and low noise in the regions of "zero" measured current, capacitive coupling contributed measurable offsets (due to the voltage ramp during spectroscopy) and oscillating backgrounds (due to V_B modulation for dI/dV measurements), which were removed during data analysis.

The first-principles DFT calculations were performed using the generalized gradient approximation (GGA) of Perdew, Burke, and Ernzerhof (PBE),¹⁷ as implemented in the SIESTA package.¹⁸ We used standard Troullier-Martin pseudopotentials for the description of C and Cu (respectively, 4 and 11 electrons) taken from the Siesta pseudopotential database. The electronic density was represented on a 300 Ry grid and converged to 10⁻⁵ number of electrons. Brillouin zone integrations were performed using an electronic temperature of 0.05 eV, a $4 \times 4 \times 1$, $4 \times 2 \times 1$, and $2 \times 2 \times 1$ k-point grid for the calculations at full, half, and quarter coverage, respectively. Our structural approximant consists of two C₆₀ molecules deposited on a 6-layer-thick slab of Cu (16 Cu atoms per layer at full coverage, hcp binding site) in a hexagonal unit cell (with a 10.21 Å in-plane lattice parameter, and a 60 Å lattice parameter in the direction perpendicular to the surface, corresponding to $\simeq 27$ Å of vacuum between the top-most C atom and the bottom layer of Cu). Interatomic forces were optimized below 0.04 eV/Å, while keeping the 4 bottom-most Cu layers in their bulk positions. Electronic density and density of states (DoS) were computed using a slab dipole correction along the z axis.

III. RESULTS AND DISCUSSION

In Figure 1, we show the arrangement of the C_{60} film grown as described above. The large-scale STM topographic image in Fig. 1(a) shows what appears to be dendritic growth, where close-packed directions are slightly preferred for growth, leading to large fern-shaped islands. Additionally, most islands appear to be located adjacent to or on top of a translational domain boundary, which are imaged as extended linear features (again, oriented along close-packed directions). Figure 1(b) shows a detail of the topography, with an extended translational domain boundary in the monolayer running up the middle of the image and a second-layer C_{60} island visible in the top left corner. Molecules at the edge of the second-layer C_{60} film appear larger than molecules within the island due to convolution with the shape of the tip. In Fig. 1(c), we present a model of a second layer C_{60} island atop a monolayer of C_{60} atop fully reconstructed Cu(111).

We explored the transport characteristics and spatial dependence of this molecular system by measuring 2112 I(V)curves over a 10×5.2 nm² region corresponding to the edge of the bilayer, as indicated in Fig. 1(d), where the topography is represented by square columns for each I(V) curve. By "simultaneously" performing the measurements on both the C₆₀ monolayer and the bilayer, we were able to confirm that the same tip condition was maintained for both regions; no data were filtered from this set. The tip height at each point was established at the tunneling conditions $V_B = +2.0$ V and I_t = 200 pA. The data from the monolayer (red) and the bilayer (blue) are separated by height and compiled into histograms on the left and right of Fig. 1(e), respectively; averages of the curves are overlaid as a dotted line and shown on a log scale in the inset. The rectification ratio (RR) (RR = |I(V)/I(-V)|) is computed from the average I(V)s and shown in Fig. 1(f) and serves as a figure of merit for the degree of rectification of the two molecular systems.

The monolayer of C₆₀ (left, Fig. 1(e)) on Cu shows quasiohmic behavior for $|V_B| \le 0.5$ V, with nonlinear increases in current arising at $\simeq -0.5$ V and $\simeq 0.7$ V as new conductance

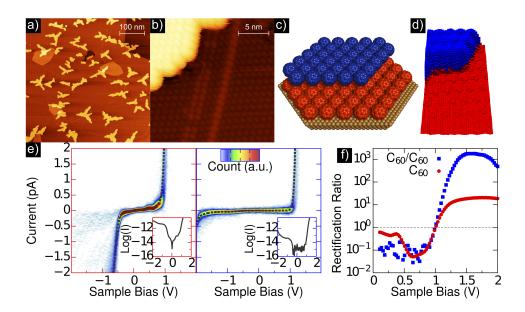


FIG. 1. (a) Scanning tunneling topograph of the C₆₀/Cu(111) bilayer (500 nm, $V_B = 1.6$ V, $I_T = 0.3$ nA). (b) Detail of the film (20 nm, $V_B = 1.63$ V, I_T = 0.22 nA). (c) A model of the film showing an ideal arrangement. The red molecules are seated on an hcp site of Cu(111): the blue molecules are in hollow sites atop the red molecules. (d) Grid spectroscopy topograph. The data are shown as square columns. each representing a I(V) curve. (e) Histograms of the I(V) curves from the red (monolayer) area (left) and the blue (bilayer) area (right). (f) Rectification ratios (RR = |I(V)/I(-V)|) of the average current-voltage characteristics for the monolayer (blue) and bilayer (red) areas.

channels appear. The associated RR dips below 0.1 at lower voltages but increases to unity at $V_B \simeq 1$ V and settles at $\simeq 20$ at higher voltages. In contrast, the I(V) characteristics in the $C_{60}/C_{60}/Cu(111)$ region are strongly non-ohmic (right, Fig. 1(e)). As can be seen in the log plot in the inset, for -0.5 $\leq V_B \leq 0.9$ V, the measured current is below the instrument noise. A weak current channel appears at $V_B \simeq -0.5$ V, but the current remains below 100 fA until $V_B \simeq -1.7$ V; as this voltage aligns with the strong conductance channel in the C_{60} monolayer, this weak current may be due to direct tunneling to that C₆₀ monolayer. At positive bias, a strong current channel turns on at $V_B \simeq 1$ V. As a result of this asymmetry, the RR for this bilayer crosses unity at $V_B \simeq 1$ V and achieves $\simeq 2000$ for $1.4 \leq V_B \leq 1.75$ V. This 100× improvement in the RR is directly a result of the current suppression at negative biases. Note that the preferred path of electrons—from acceptor to metallized molecular layer-is exactly the opposite of our previous observation, which used a donor molecule (pentacene) in the second layer.¹⁴

To understand the origin of the rectifying behavior, we turn to first-principles calculations. As pointed out in previous works, 16,19,20 C₆₀ monolayers on Cu(111) are strongly hybridized, leading to a metallic DoS and large increase in their local polarizability. As seen in Fig. 2, in the case of the C₆₀ bilayer, we find that this behavior applies solely to the layer in contact with Cu(111) and does not impact the topmost layer. First, the change in electronic density upon binding (Fig. 2(a))

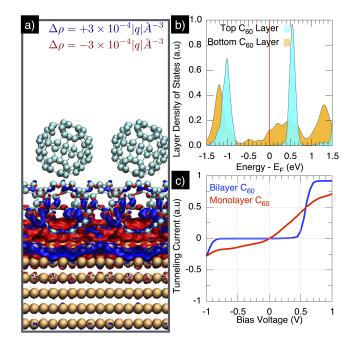
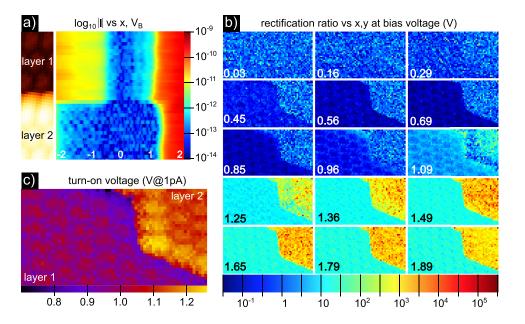


FIG. 2. Electronic structure of $C_{60}/C_{60}/C_{0}(111)$. (a) Isosurface of electronic density difference $(\Delta\rho)$ between $C_{60}/C_{60}/Cu(111)$ and its individual components $(\rho_{C_{60}}/C_{00}/Cu(111) - \rho_{C_{60}}/C_{60} - \rho_{Cu(111)})$. The change in electronic density is localized to the first C_{60} layer and the two topmost Cu layers. (b) Kohn-Sham density of states (DoS) of $C_{60}/C_{60}/Cu(111)$ projected on the two C_{60} layers. Upon binding, the bottom C_{60} layer has a metallic DoS, while the top C_{60} layer remains semiconducting. (c) Corresponding I(V) characteristics using the Kohn-Sham DoS (the Cu-DoS is assumed to be independent of energy in the energy range considered, see main text) for the monolayer (red) and bilayer (blue). The computed I(V) characteristic of the bilayer is diodic due to the top C_{60} layer preserved n-type semiconducting character and the continuous DoS in the bottom layer.

is entirely localized to the bottom layer. Moreover, as shown in Fig. 2(b), this leads to a system with a DoS reminiscent of a Schottky diode, in which the top layer remains a semiconductor with an electron-accepting character, while the bottom C_{60} layer is a metal. Interestingly, despite the original energy alignment between the lowest unoccupied molecular orbitals (LUMO) of the two C₆₀ layers, the Kohn-Sham LUMO of the top layer is found to sit at 0.58 eV above the Fermi energy. We attribute this energy mismatch to the interface dipole at the C_{60} /Cu interface, which increases the electrostatic potential^{21,22} above the negatively charged C_{60} layer. We note that this effect has also been observed for smaller charge transfer in the case of C₆₀ bilayers on Au(111).^{23,24} The increase of the electrostatic potential also suggests that molecules on top of C_{60} /Cu will have their highest occupied molecular orbital (HOMO) pushed towards the Fermi energy, in agreement with our experimental findings that the HOMO of pentacene lies 0.25 eV below the Fermi energy on top of C_{60}/Cu^{14} —which may suggest that very low onset voltages are achievable for electron-blocking layers on top of C_{60}/Cu .

The functional form of the I(V) characteristics can be understood as resulting directly from the unusual DoS of the system using the same hypotheses as in the pentacene/ C_{60} /Cu system.¹⁴ Specifically, in Fig. 2(c), we plot the Landauer current obtained when the transmission function is the product of the layer-projected DoS ($I(V) \propto$ $\int_{0}^{V} dE \text{DoS}_{\text{top}}(E) \text{DoS}_{\text{bottom}}(E)$, where V is the potential of the tip and E the energy). This formula neglects bias-induced changes in the DoS (see below) and possible direct coupling between (1) the top C_{60} layer and Cu and (2) the tip and the bottom C₆₀ layer. The calculated current has the same diodic lineshape as the one observed in experiments with a smaller onset bias (0.58 V as compared with $\simeq 1.0$ V found experimentally) that we attribute to the erroneous Kohn-Sham level alignment (because the onset voltage in the forward direction is related to the energy difference between the frontier molecular orbital and the Fermi energy of the system). Finally, we note that the spectrally broad LUMO of the bottom C₆₀ layer effectively acts in a manner similar to a *gateway* state²⁵ from the point of view of the top C₆₀ layer. While these states were found to dominate the low-bias I(V) for conjugated and nonconjugated molecules,²⁵ the weak coupling between the two C_{60} layers results in a different behavior.

We now explore the spatial and coordination dependence of our observations. In Fig. 3, we show data derived from the grid spectroscopy presented in Fig. 1. The variation in the local I(V) at the interface of the bilayer and monolayer is shown in Fig. 3(a), where the data are spatially averaged over 10 points parallel to the edge of the bilayer. In contrast with the metallic behavior of the C_{60} monolayer, and in agreement with our theoretical findings, the bilayer shows a larger "turn-on" voltage as well as reduced current in the reverse direction. The local variation of the rectification ratio is shown in Fig. 3(b). Consistent with the average rectification analysis, the local rectification shows that the monolayer is weakly rectifying with a maximum RR of about 20, while the bilayer is strongly rectifying with local maximum RR up to about 10^4 . Interestingly, we find that, while the rectification ratio is homogeneous in the bilayer, the turn-on voltage is strongly dependent on the



distance from the edge of the island and the local intra-layer coordination (e.g., $V_B = 1.09$ V, Fig. 3(b)).¹⁴

Such behavior is particularly noticeable around 1 V, where the edge of the bilayer starts rectifying. A summary of these phenomena is shown in Fig. 3(c), which shows the spatial dependence of the turn-on voltage (as defined by the voltage

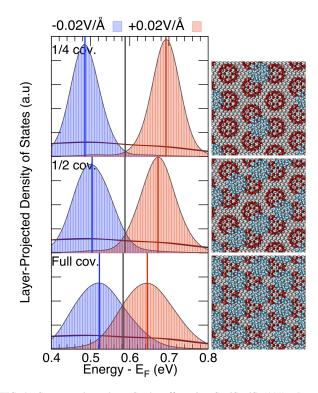


FIG. 4. Coverage-dependent Stark effect in $C_{60}/C_{60}/Cu(111)$. Layerprojected DoS from DFT of molecules at quarter (top panel), half (middle), and full (bottom) coverage for the top C_{60} layer. Red and blue curves correspond to the DoS under fields of opposite polarities for the top (filled curves) and bottom (plain lines) layers. Only the top layer DoS is affected by the electric field. Blue, black, and red vertical lines correspond to the maxima of the Gaussian fit of the top layer DoS for the negative, 0-, and positive field cases, respectively. Larger orbital Stark shifts are found at lower coverage. Corresponding structural models used in the DFT calculations are shown on the right.

FIG. 3. Scanning tunneling spectroscopy of $C_{60}/C_{60}/Cu(111)$. (a) $\log_{10}|I(V)|$ traveling across a step between the bilayer and the monolayer, with lateral averaging over 10 points. (b) *RR* maps for the entire bias range, showing zero rectification at low bias and strong rectification for biases above 1.2 V. The strongest rectification is at 1.6 V. (c) Map of "turn-on" voltage for the system, showing that the turn-on voltage decreases with increasing coordination of the C₆₀ molecule.

needed for the current to be larger than 1 pA). Such turnon voltage varies from 1 V for the C_{60} molecules within the island (2d coordination 6) to 1.2 V and 1.25 V for those on the edges (2d coordination 4) and the molecule at the corner (2d coordination 3), respectively.

While the number of atoms involved prevents a direct DFT calculation of the electronic structure of the edge and corner molecules, we examine the differences between the fully covered bilayer of C_{60} on Cu(111) and the half- and quarter-coverage situations (coverage referring to the second C_{60} layer). In Figure 4, no significant change is found in the top layer's LUMO energies for the three coverages (within 0.01 eV of each other, as determined by a Gaussian fit of the layer-projected density of states). However, we observe more significant differences in the molecular orbital energies response to an external electric field, i.e., a larger orbital Stark effect as coordination is reduced. Specifically, when applying electric fields of ± 0.02 V/Å perpendicular to the surface (Fig. 4), we find the energy shift of the LUMO to be 70% and 38% larger in the quarter- and half-coverage cases (±103 meV and ± 83 meV, respectively, as compared with ± 61 meV for the full coverage case) due to the change in local dielectric environment. While the structural and field models both differ from the experimental conditions, the computed magnitude of this effect is compatible with the experimental observation of a 15%-20% increase of the "turn-on" voltage at the edges. Moreover, as pointed out in Ref. 26 in the context of C₆₀ monolayers and molecules on Au(111), changes in local dielectric environment are also conducive to impacting the level alignment through non-local static correlations-an effect beyond the reach of standard DFT approaches.²⁷ Both Stark effect and level alignment renormalization result in the same qualitative behavior: the measured LUMO energy increases at lower coordination. Further STS studies on the dependence of the measured LUMO energies on the tip-substrate distance should allow the determination of the relative magnitude of these two mechanisms.

In conclusion, we have observed large rectification ratios in non-covalent, self-assembled, molecular bilayers of C_{60} on

Cu(111). Using DFT, we have shown that, due to its strong coupling with Cu(111), the bottom C_{60} layer acts as a metallic buffer layer, preserving the semiconducting character of the top C_{60} layer while allowing electron and hole injection. We have analyzed the local variation of the rectification and found that C_{60} molecules with smaller coordinations have larger turn-on voltages, a phenomenon we attribute to an enhanced electronic Stark effect in a local environment with reduced dielectric screening.

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