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# *Article* 1 **Optimising Flowback Strategies in Unconventional Reservoirs:** <sup>2</sup> **The Critical Role of Capillary Forces and Fluid Dynamics** <sup>3</sup>

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Abstract: This study delves into the complexities of fluid cleanup processes post-hydraulic fractur- 9 ing in unconventional gas deposits, focusing on the pivotal role of capillary pressure (Pc) correla- 10 tions in tight and ultra-tight formations. Utilising the Geo2Flow software, the research evaluates the 11 efficacy of existing Pc models, identifying the Brooks & Corey model as notably precise for these 12 formations, albeit recommending an adjustment to the pore size distribution index for a more accu- 13 rate representation of rock behaviours. Further investigation centres on the cleanup process in mul- 14 tiple fractured horizontal wells, examining the impact of Pc, matrix permeability, drawdown pres- 15 sure, and fracturing fluid volume. A significant portion of the study addresses the influence of in- 16 terfacial tension-reducing chemicals on post-fracturing production, highlighting their utility in ul- 17 tra-tight formations but advising against their use in tight formations due to environmental con- 18 cerns and limited efficacy. The findings underscore the nuanced interplay between geological pa- 19 rameters and fracturing fluid dynamics, advocating for tailored fluid cleanup strategies that en- 20 hance hydraulic fracturing efficiency while minimising environmental impact. This comprehensive 21 analysis offers valuable insights into optimising fracture cleanup and understanding the underlying 22 physics, thereby contributing to more effective hydraulic fracturing practices. 23

**Keywords:** Flowback cleanup; Hydraulic Fracturing; fracturing fluid; Capillary pressure; IFT; un- 24 conventional reservoirs. 25

# **1. Introduction** 27

The least polluting and emitting fossil fuel is thought to be natural gas. Due to its 28 abundance and environmental sustainability, it is also regarded as one of the most signif- 29 icant energy sources in the future. Around the world, using natural gas is becoming in- 30 creasingly significant in producing electricity, industrial processes, and domestic heating. 31 Resources for natural gas are either conventional or unconventional. Despite being less 32 economically viable than conventional natural gas reserves and more challenging to ex- 33 tract, there is a rising reliance on unconventional gas resources to meet the world's energy 34 demands. Shale gas, gas hydrates, tight and ultra-tight gas sands and coalbed methane 35 are all sources of unconventional gas plays. The considerable rise in gas consumption has 36 led to the development of further unconventional resources[1–3]. 37

Fracturing, or hydraulic fracturing, is a prevailing technique for increasing the pro- 38 duction of wells in unconventional gas reserves. With this technique, the rock formation 39 is fractured by pumping a mixture of water, chemicals and sand into the well under sig- 40 nificant pressure. Different companies have widely adopted Fracturingor, which extracts 41 large quantities of natural gas from unconventional deposits, but it has also been met with 42 opposition due to environmental and health concerns[4–13]. 43

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Shale gas and tight gas sands are gaining popularity among unconventional re- 44 sources. Conversely, conventional natural gas reserves are exhausted because of their 45 availability and relative ease of access [14–20]. 46

The potential benefits and disadvantages of natural gas unconventional resources 47 need to be weighed against the larger picture of global energy demands and environmen- 48 tal concerns. The environmental impact of extracting unconventional gas resources and 49 the possible health implications must be handled and examined, notwithstanding the re- 50 source's promise as a supply of natural gas. Companies and governments are developing 51 new technologies and laws to meet energy demands while lowering their negative effects 52 on the environment. Unconventional resources, thus, play a progressively essential role 53 in addressing global energy demands, notwithstanding the difficulties they provide com- 54 pared to conventional reserves. Technologies and techniques, such as hydraulic fractur- 55 ing, are being developed to enhance the production of unconventional gas resources while 56 minimising environmental impact. As the world continues to face energy challenges, it is 57 crucial to consider the potential benefits and drawbacks of unconventional natural gas 58 resources in the context of the bigger picture of global energy demands and environmen- 59 tal concerns  $[14-20]$ . 60

Injecting large amounts of fracturing fluid, or FF, allows for initiation and propagat- 61 ing cracks in unconventional reservoirs $[21–26]$ . In the tight oil and gas sectors, vertically 62 drilled, hydraulically fractured wells have first been drilled in Pennsylvania, a state in the 63 northeastern United States. Numerous experimental, computational, and field studies 64 have been conducted to determine how hydraulic fracture cleanup effectiveness affects 65 phase production in unconventional tight/ultra-tight formations [21,22]. Numerous field 66 experiments have demonstrated how considerably gas output can be hampered by inad- 67 equate FF removal.[27,28]. 68

The physical characteristics of the FF, the formation's characteristics, and the hydrau- 69 lic fracturing operation's design all affect the volume of the flowback. 10 to 70 percent of 70 the entire volume of the initially injected FF could make up for the flowback recovered 71 from the well at the surface[29,30]. More FF is often retained in the formation. Therefore, 72 when the formation has some micro fractures and higher matrix capillary pressures, sur- 73 face flowback recovery is reduced [29,30]. 74

The oil and gas sector now emphasises optimising the fracturing fluid flowback for 75 a number of purposes such as maximising net profit and addressing environmental con- 76 cerns. Some techniques mitigate FF flowback using a Tech-Flo hydraulic jet pump to max- 77 imise load recovery [31]. Simultaneously isolating the hydrocarbon from the well stream 78 helps hasten the safe recovery of a substantial flowback. A flowback service for multiple 79 fractured horizontal wells (MFHWs) in unconventional fields has also been made availa- 80 ble by Halliburton[32]. CALIBR, a service offered by a company called CALIBR, aims to 81 boost well performance by reducing completion damage and maximising long-term out- 82 put. The service enhances productivity and completion efficiency by continuously moni- 83 toring, analysing, and controlling flowback. Through the use of CALIBR, hazardous flow- 84 back procedures can be avoided, the damage in fracture permeability can be reduced, and 85 the performance of the well can be improved. This is achieved by continuously monitor- 86 ing well pressure, assessing well performance, and adjusting the choke in real-time. CAL- 87 IBR, a flowback operation service by Halliburton, enhances well performance by reducing 88 completion damage and maximising long-term output. This service employs real-time 89 monitoring and analysis using high-resolution pressure gauges like SPIDR®, allowing for 90 precise adjustments to flowback processes based on continuous data acquisition. Each 91 flowback plan is customised to the well's specific characteristics, incorporating its design, 92 previous completion activities, and field knowledge to optimise productivity and mini- 93 mise damage. Through an iterative process of continuous measurement, analysis, and 94 choke adjustment, CALIBR avoids aggressive flowback strategies that could damage frac- 95 ture conductivity, thus maintaining well performance. Additionally, the service mitigates 96 potential damage-causing practices, reducing the risk of issues such as proppant washout 97

and fines migration. Overall, CALIBR's comprehensive, data-driven approach to flow- 98 back management maximises the economic value and long-term productivity of wells[32] 99 . Holditch [25] studied how the productivity of fractured wells is affected by the growth 100 of fluid saturation (FF), which is assumed to be water, and the reduction of permeability 101 in the area near the fracture. His goal was to determine the impact of damage to the grid- 102 like structure surrounding the fracture. He used a numerical simulator based on finite 103 differences to conduct his research. It was found that in low-pressure drawdown condi- 104 tions, where the drawdown pressure (DP) was only slightly greater than the capillary 105 pressure (Pc) of the matrix in tight formations (reservoirs with low permeability), the ef- 106 fect of capillary pressure was significant. He pointed out that water blocking takes place 107 when the matrix permeability(km) around the fracture declines by 99.9%, or when the 108 differential pressure (DP) is less than the capillary pressure (Pc) in the region where the 109 fracturing fluid (FF) has penetrated. The invasion depth of the FF in their matrix extended 110 up to 5 inches, and its distribution within the matrix adjacent to the hydraulic fracture 111 was consistent. His study did not examine the impact of FF volume on the conductivity 112 of the fracture. 113

Decline in expected gas production is a complex process involving several factors, 114 including matrix permeability damage caused by two-phase flow and the efficacy of 115 cleaning up single fractured vertical wells. To understand these factors, researchers have 116 conducted extensive studies that have shed light on the underlying mechanisms that af- 117 fect gas productivity. 118

One important finding is that Pc and Kr in invaded zones are important factors in 119 cleanup effectiveness in low-permeability reservoir rocks. This conclusion was drawn by 120 Pope et al. in 1996, who determined a direct correlation between gas flow and flowback 121 recovery by analysing data taken from the field. They suggested that when the liquid is 122 produced from the hydraulic fracture, a corresponding space opens up, allowing gas to 123 flow towards the well. As load recovery increases, gas production also upsurges. To fur- 124 ther investigate this, they examined the dependency of gas rates on flowback and advised 125 that higher flow rates leads to higher load fluid recovery. 126

Following their investigation, Gdanski et al. [28] examined the formation damage 127 caused by gas and fluid flow in the invaded zone and established a numerical model. They 128 noticed that damages in the fracture sand face significantly lower gas productivity if the 129 permeability of the matrix in the invaded zone is reduced to 1% of the original permeabil- 130 ity. However, they overlooked that higher Pc results in more fluid being absorbed into the 131 matrix, which lowers fluid saturation within the frack, increases the permeability of gas 132 within the fracture, and produces cleaner fractures. 133

The next important factor in gas production is the effectiveness of cleaning up frac- 134 tured wells. Ghahri et al. investigated this issue in 2009 and understood that cleaning up 135 such wells in gas fields efficiently enhances gas productivity. Their findings were based 136 on a numerical simulations and detailed analysis of field data and they proven that clean- 137 ing up single fractured vertical wells can lead to significant improvements in gas recovery. 138

These findings highlight the complex nature of gas production and the need to un- 139 derstand the underlying mechanisms that affect productivity. By building on the work of 140 earlier researchers, current and future studies can continue to shed light on this important 141 issue, aiming to improve gas recovery and meet the world's growing energy needs. 142

Additionally, they replicated the numerically developed model outcomes that 143 Holditch (1979) indicated, which have since been used as a reference in several cleanup 144 simulation investigations[25]. According to their findings, the presence of FF in the zone 145 that has been invaded influences the total amount of gas recovery by diminishing the rel- 146 ative permeability of the gas, which reduces gas rate when in contrast to a scenario in 147 which FF was not pumped into the well. More significant FF recovery occurs during pro-<br>148 duction when FF viscosity is reduced and, as a result, FF mobility is increased. They also 149 emphasised that as Pc rises, the FF penetrates deeper into the matrix, improving gas pro- 150 duction and reducing FF interference. 151

Ghahri et al (2011) expanded on this study by thoroughly examining 16 important 152 parameters while utilising experimental design and a surface model [33]. They showed 153 that the parameters relating to the FF cleanup within the fracture, particularly kf, had a 154 considerable impact on gas production loss, or GPL[33]. 155

The central processing unit (CPU) time needed for these two numerical experiments 156 was excessive [33]. As a result, the authors could only examine two simulation sets. Ja- 157 miolahmady et al. (2014) conducted additional research on flowback cleanup processes. 158 They simplified the model by reducing the number of parameters from 16 to 12 by remov- 159 ing four parameters that had minimal impact on the cleanup performance. This made it 160 easier to explore more diverse cleanup scenarios. 161

The study that was conducted by Ghahri et al (2011) focused on different factors that 162 included the size of the pores, the force between interfaces, how easy it is for substances 163 to pass through the matrix and fracture, and the way that fluids move through these struc- 164 tures. The study was expanded to cover a wider variety of cleanup situations in gas res- 165 ervoirs that are extremely tight. To achieve this, researchers ran eighty-four simulations 166 that considered various factors, such as the amount of fluid injected, the duration of the 167 soak, the pressure at the bottom of the well, and the compactness of the formation [33]. 168

The study revealed that the cleanup process becomes slower and gas production loss 169 becomes more significant as the formation becomes tighter (i.e., smaller km). Likewise, 170 the study demonstrated that when the pressure drawdown was low, the capillary pres- 171 sure (Pc) more significantly impacted the efficiency of the cleanup process than before. A 172 similar result was obtained when the soaking period was increased. Nasriani and col- 173 leagues have conducted several studies on enhanced oil recovery, investigating various 174 techniques and strategies ([29,30,34–39]), while more recent works by Modebelu et al. 175  $(2022)$  & Erimako et al. (2022) have focused on particular aspects of the process [40,41]. 176 Nasriani et al. (2018) studied various factors impacting post-fracturing cleanup effective- 177 ness [30,36]. The study considered several variables, such as the length of the fracture, 178 well pressure, hysteresis, segregation due to gravity, mobility, immobility of the connate 179 water, and volume of the injected fracture fluid. The results of the investigation revealed 180 that particular outcomes may arise when a considerable quantity of fracture fluid is in- 181 jected into formations with extremely high permeability, it significantly reduces gas flow 182 and severely slows the cleanup procedure. Extending the soaking time or increasing the 183 pressure drawdown did little improve GPL in this situation. The researchers found that 184 hysteresis did not significantly affect the efficiency of the cleanup process. The examina-185 tion of cleanup performance was extended to explore the influence of layered systems, 186 and it was discovered that capillary pressure plays a more crucial role in the bottom layer 187 than in the top layers. Additionally, The mobility coefficient of the fluid in the fracture is 188 higher in the upper layer than in the lower layer. Furthermore, they suggested that using 189 an IFT reduction agent during fracturing operations could reduce gas production losses 190 in reservoirs with high water saturation levels. 191

Nasriani and Jamiolahmady (2019) expanded the research scope to include studies to 192 conduct to examine the cleanup procedure that takes place after hydraulic fracturing in 193 wells with multiple horizontal fractures [29]. 194

More precisely, the effect of wide-ranging horizontal lengths and fracture spacing in 195 MFHWs on cleanup efficiency was studied. Furthermore, the researchers compared the 196 cleanup processes after fracturing in vertical wells (VWs) and MFHWs. Running the nu- 197 merical simulation for the sets consumed considerable CPU time. 198

In an effort to mitigate the significant computational burden associated with simula- 199 tion runs using full factorial sampling (FFS) experimental design and to accelerate the 200 computational process, researchers have adopted an alternative approach known as Latin 201 Hypercube Sampling (LHS). This novel sampling technique has emerged as a promising 202 solution for conducting high-dimensional experiments with fewer runs, thereby reducing 203 the overall CPU time required for simulation. They observed a difference in the trend of 204 km values between the base reference set and the VW Set for multiple fractured horizontal 205

According to these results, FF production was more adversely impacted gas produc- 212 tion in the set. In simpler terms, a greater Pc in MFHWs is more significant since it causes 213 more FF to get more absorbed into the rock and less opposition to gas passage. It was also 214 demonstrated that MFHW cleaned up more quickly than VW. This resulted from sets hav- 215 ing a greater gas production rate. Slower (faster) cleanup was seen in Reduced (Increased) 216 DP MFHW settings, comparable to those formerly reported for the related VW sets. They 217 concluded that while fracture interference and fracture spacing substantially impact flow, 218 they have little effect on cleanup performance in MFHWs with varying spacing between 219 fractures. 220

Recent advancements in hydraulic fracturing and unconventional gas extraction 221 have significantly contributed to the efficiency and productivity of shale gas reservoirs. 222 For instance, characterising anisotropic geomechanical properties through nanoindenta- 223 tion and upscaling approaches provides a deeper understanding of formation behaviour, 224 which is critical for optimising hydraulic fracturing treatments [42]. Additionally, compu- 225 tational analyses of proppant transport and screen-out phenomena have highlighted the 226 complex interactions within fractures, leading to more effective fracturing strategies [43]. 227 Experimental studies on the stable dispersion of coal fines during hydraulic fracturing 228 flowback emphasise the importance of addressing particle mobilisation to enhance 229 cleanup efficiency [44]. Furthermore, probabilistic quantification of microparticle segre- 230 gation under electrostatic forces has provided new insights into preventing screen-out 231 during fracturing operations [45]. Innovative techniques such as co-applicating indirect 232 hydraulic fracturing and micro-proppants have improved pre-drainage in low permea- 233 bility coals, highlighting the ongoing efforts to enhance gas recovery in challenging for-<br>  $mations [46]$ . 235

Moreover, the integration of machine learning in reservoir management has opened 236 new avenues for predicting production and optimising resource extraction. Srinivasan et 237 al. (2021) demonstrated the potential of machine learning-assisted history matching and 238 production forecasting in shale gas reservoirs, which can significantly improve decision- 239 making processes and operational efficiency [47]. These recent studies collectively under- 240 score the critical role of technological advancements and interdisciplinary research in ad- 241 dressing the challenges of unconventional gas production, thereby supporting the grow- 242 ing global energy demands while mitigating environmental impacts. 243

This study aims to enhance the existing knowledge of hydraulic fracturing treat- 244 ments for real-world applications by building on prior research [3,14,15,20,30,31]. It spe- 245 cifically explores the influence of unconventional Pc on the performance of MFHWs. This 246 paper presents an in-depth analysis of Pc correlations applicable to tight and ultra-tight 247 formations, utilising the Geo2Flow software. Geo2Flow is an advanced numerical model-<br>248 ing framework that integrates petrophysical, geological, engineering, and geophysical 249 data to accurately simulate groundwater flow and solute transport in porous media. By 250 matching 3D saturations to well logs, calculating precise 3D permeabilities, and identify- 251 ing reservoir compartments, Geo2Flow enhances the accuracy of reserve estimations and 252 subsurface models. Its interdisciplinary approach and robust algorithms ensure that it 253 handles both data-rich and data-poor environments effectively, making it a valuable tool 254 for environmental engineers and researchers[48]. 255

Analysis of the Pc model, applied to 200 datasets from conventional, tight, and ultra- 256 tight formations, proved that the Brooks & Corey model, with just one specific parameter, 257 effectively represents Pc data for unconventional plays. Results from this research recom- 258 mend constraining the pore size distribution index  $(\lambda)$  to a 0.3–1.5 range for a more 259

accurate portrayal of unconventional rock properties. The updated  $\lambda$  range was incorpo- 260 rated into the model to more accurately represent the unconventional Pc characteristics. 261

Additionally, for these five data sets, a novel dimensionless terminology—analogous 262 to gas production loss (GPL)—was introduced to study the influence of similar key pa- 263 rameters on FF production, which is a significant factor in the HF of unconventional res- 264 ervoirs. 265

### **2. Methodology** 266

A flowchart is used in this part to clarify the adopted analysis methodologies and 267 terminologies, as shown in Figure 1. A comprehensive assessment of capillary pressure 268 (Pc) correlations for tight and ultra-tight formations has been conducted.This analysis uti- 269 lised the Geo2Flow software to examine the dependability of existing Pc correlation mod- 270 els specifically for these formations [41,48]. Then, it was decided that Pc data would be 271 best represented by Brooks and Corey's model. in unconventional plays. However, it was 272 proved for the first time that the  $\lambda$  range for unconventional resources used in the Brooks 273 and Corey model must be adjusted to 0.3 to 1.5, rather than 1 to 4 previously used in 274 previous works [30]. This Pc formulation adjustment improves capillary forces' represen- 275 tation in unconventional tight/ultra-tight rock formations more realistically. Then, a mul- 276 tiple horizontal fractured well model initially created by [29] was utilised for sets. The 277 dimension of the model is shown in Table 1; the validation procedure of the modified 278 MFHW model is discussed elsewhere. [30]. 279

Once the MFHW model is validated, five scenarios are considered. The five different 280 scenarios are: 281



It should be highlighted that each set consists of 1000 simulation runs in which the 287 12 pertinent parameters are varied within their variation range. The range of all pertinent 288 parameters is shown in Table 2. A full explanation of the sampling approaches used in 289 this work can be found elsewhere [29]. All scenarios used Latin Hypercube Sampling 290 (LHS) to generate the required simulation runs, and then mathematical surface method- 291 ology was used to match an accurate model to the results from each set. Finally, results 292 from these sets were examined. A list of sets that have been analysed is shown in Table 3. 293







### *2.1 An in-depth assessment of Pc formulas in unconventional plays.* 302

his section presents the findings from a comprehensive analysis of different Pc cor- 303 relations applied to unconventional formations, utilising the Geo2Flow software. [39]. For 304 this research, 200 Pc data sets, collected from tight and ultra-tight formations in western 305 U.S. basins, were examined, with measurements provided by the University of Kansas 306 Center for Research and presented to the U.S. Department of Energy [40]. 307

The study specifically examined various J-function models to investigate capillary 308 force irregularities in tight and ultra-tight sands. This part discusses the initial and 309 adapted Leverett J-functions , other J-function models, and the associated fit error indica- 310 tors as applied to these unconventional formations. 311

#### 2.1.1.The Leverett J-function 313

Leverett (1941) showed that in reservoir rocks with identical lithology but varying 314 porosity and permeability, capillary pressure could be normalised using a single function 315 known as the Leverett J-Function. Rather than plotting Pc against Sw, Leverett instead 316 used the J-Function, as detailed in Equation 1 [41]. 317

$$
J(S_w) = \frac{P_c}{\gamma \cos \theta} \sqrt{\frac{k}{\varphi}}
$$

Where  $\gamma$  is the Surface tension,  $\theta$  is Contact angle, k is the Permeability and  $\varphi$  is the 318 Porosity. 319

According to Leverett's method, a small set of J-functions can effectively represent 320 the Pc characteristics across the rocks within an entire reservoir. Leverett's findings imply 321 that, for a specific rock type, most Pc curves can align with one J-function. Essentially, one 322 J-function can encompass multiple Pc curves. 323

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the threshold value that the non-wetting phase must surpass to penetrate the rock is 326 represented by the J-function displacement, Jd. This value aligns with the displacement 327 pressure,  $P_d$  (also referred to as threshold pressure,  $P_e$ ), as outlined in Equation 3.6 on the 328 Pc curve. When P<sub>d</sub> is substituted into Equation 5.1, J<sub>d</sub> is obtained. In this study, all P<sub>c</sub> func- 329 tions are dependent on Jd, as it establishes the location of fluid contacts. 330

# 2.1.3. The Model proposed by Thomeer 332

In 1960, Thomeer demonstrated that plotting the logarithm of capillary pressure 333 against the logarithm of saturation of non-wetting phase produces a hyperbolic curve.He 334 introduced a J-function model, detailed in Equation 2 [42], to represent this relationship. 335

$$
S = 1 - 10^{-\frac{G}{Log(\frac{L}{f_d})}}
$$

Where S is reduced saturation,  $J_d$  is J-function displacement,  $J$  is the J-function value 336 and G is the Pore geometric factor. 337

### 2.1.4. The J-function Model proposed by Brooks-Corey 339

 Brooks and Corey (1966, 1964) developed a model using a bundle of capillary tubes 340 to characterize a porous media, introducing the following terms [49,50]: 341

$$
S = \left(\frac{J_d}{J}\right)^{\lambda} = \left(\frac{J_d}{J}\right)^{1/a_0} \tag{3}
$$

Equation 5.3 corresponds to Equations 3.6 and 3.7 on the capillary pressure curve. 342

# 2.1.5 The J-function Model proposed by Bentsen-Anli 344

Bentsen and Anli (1977) suggested a J-function model introduced by Eq[.4](#page-9-0) [51]. 345

$$
= e^{\left(\frac{d-1}{a_0}\right)}
$$

# 2.1.6. The model of Skelt-Harrison 347

 $\overline{S}$ 

Skelt & Harrison (1995) proposed a J-function model characterized by two specific 348 parameters, detailed in Equation 5 [46]. In contrast to the previous models, this model 349 uniquely incorporates two parameters: a0, serving as the scaling factor for Pc, and a1, 350 which functions as the exponent for the scaled Pc.  $351$ 

$$
S = 1 - e^{-\left(\frac{a_0}{f - f_d}\right)^{a_1}}
$$

Skelt and Harrison first presented their model relating height above the free water 352 level and Pc. Reformulating this relationship through the J-function yields Equation 5. 353

# 2.1.7. O'Meara Unimodal J approch 355

Similar to the the Skelt-Harrison J-function model, the O'Meara Unimodal J-function 356 model incorporates two distinct parameters of a0 and a1, and is represented by Equation 357 6.  $\frac{358}{255}$ 

$$
S = \frac{1}{2} \operatorname{erfc} \left( \frac{Log(\frac{1 - f_d}{a_0})}{a_1} \right)
$$

In O'Meara's model, the erfc function denotes the complementary error function. This 359 model is characterized by two distinct parameters: a0, which signifies the median of the 360 associated lognormal distribution, and a1, which indicates the variance of that distribu- 361 tion. 362

# *2.2. Analysis of Pc Correlations* 364

To evaluate the appropriateness of specified Pc correlations for ultra-tight rocks, 200 365 Pc datasets were integrated into Geo2Flow. In Geo2Flow software [39], data fit quality is 366

determined through either the the least absolute deviations approach or least squares 367 technique, with both assessed by an 'error in fit.' This error metric, applied to n data points 368 (xi, yi) following the function  $y = f(x)$ , is calculated as the sum of squared deviations be- 369 tween actual data points and their corresponding values when using the least squares 370 method, as outlined in Equation 7 371

$$
\Delta = \sum_{i=1}^{n} [y_i - f(x_i)]^2
$$

 $\frac{l}{l}$  In the case of the least absolute deviations (LAD)approach, the error is defined as the 372 total of the absolute differences between the data points and their respective correspond- 373 ing values, as indicated by Equation 8: 374

$$
\Delta = \sum_{i=1}^{n} |y_i - f(x_i)|
$$

 =1 Notably, a lower Δ value indicates an improved curve fit. This work utilised the least 375 squares method (LSM). For this task, all datasets were initially formatted in Excel to align 376 with the requirements of Geo2Flow before importing into the software. Five different 377 models were examined: Figure 2 illustrates the imported PC data sets in relation to satu- 378 ration, with Pc expressed in Bar. The corresponding J-functions, derived using specific K, 379 φ, IFT, and contact angle values, are displayed in Figure 3. 380



Five different models were evaluated: three single-parameter models (Brooks & Co- 381 rey, Thomeer and Bentsen & Anli) and two dual-parameter models (Skelt-Harrison & 382 O'Meara Unimodal). The Pc data sets were fitted using the least squares method (LSM), 383 with the associated fit error values for each model outlined in Table 4. For the full data 384 set, Table 4 presents the error values for the the five models. The Thomeer model, notably, 385 provided the most accurate fit, while the Bentsen and Anli model had the highest error 386 when assessing all data. Models with dual parameters generally produced more precise 387 Pc predictions due to their greater adaptability; however, the Thomeer model, despite be- 388 ing a single-parameter model, performed better than many others. The Brooks and Corey 389 model was the second most accurate among the single-parameter models.To improve the 390 assessment of these models' reliability in unconventional formations, the Pc data sets were 391 divided into three categories: conventional  $(k > 0.1 \text{ md})$ , tight  $(0.001 \le K \le 0.1 \text{ md})$ , and 392 ultra-tight  $(K < 0.001$  md), with the conventional data sets being excluded from further 393 analysis. The LSM was reapplied to the unconventional data, and the resulting error val- 394 ues for each model are shown in Table 4. For tight Pc data, Table 4 includes the error 395 values for the Thomeer, Brooks & Corey, Bentsen & Anli, Skelt-Harrison, and O'Meara 396 models. The Brooks & Corey model was found to be the most accurate among single- 397 parameter models, while the Skelt-Harrison model performed best among dual-parame- 398 ter models. For ultra-tight Pc data, the error values in Table 4 indicate that Brooks and 399 Corey, along with Thomeer, were the best-performing single-parameter models, while 400 Skelt-Harrison and O'Meara Unimodal were superior among dual-parameter models. Ta- 401 ble 4 also shows that the Bentsen and Anli model was the least accurate for both tight and 402 ultra-tight Pc data sets, while the Brooks & Corey model was the most effective for these 403 unconventional categories. 404

# **Table 4** Error in fit analysis 407



#### 2.2.1. Evaluation of the Brooks & Corey Model 409

The results demonstrated that the Brooks & Corey model effectively fits both tight 410 and ultra-tight data sets. The evaluation of five distinct J models was conducted for Pc 411 data sets for tight formations (0.001 md < K < 0.1 md) and Pc data sets for ultra-tight (K <  $412$ 0.001 md), as described in Section 5.2. A range of data sets from these categories was ana- 413 lyzed. For each data set, the Brooks and Corey model was applied to ascertain the typical 414  $\lambda$  characteristic of these unconventional data sets. The findings showed that the Brooks & 415 Corey model accurately represents both tight and ultra-tight data sets. 416

**Table 5** The  $\lambda$  analysis 418

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Table 5 displays a selection of the evaluated data, detailing the sample data set 420 names, K,  $\varphi$ , estimated  $\lambda$ , J-function displacement, and curve fitting error metrics. The 421 estimated  $\lambda$  for these samples span from 0.313 to 1.49. To demonstrate the high correlation 422 between the Brooks & Corey model and observed data, two specific sample data sets were 423 chosen: a tight and an ultra-tight data set. 424

A data point from the tight data group, has a permeability (K) of 0.0086 md and a 425 porosity of 11.8%, with an error in fit of 2.06E-3, indicating minimal deviation. Figure 4 426 illustrates a close match between the Brooks  $&$  Corey model fit and the actual data for this 427 set, showing a  $\lambda$  of 1.08 and a J-function displacement of 0.054. The ultra-tight sample, has 428 a permeability (K) of 0.00016 md and a porosity of 3%, with an error in fit of 1.99E-4, 429 suggesting an excellent fit. Figure 5 illustrates an almost exact alignment between the 430 Brooks & Corey model fit and the observed data, characterised by a  $\lambda$  of 0.67 and a J- 431 function displacement value of 0.055. 432

#### 2.2.2. Concave down effect 434

Certain Pc (or Leverett J) curves exhibit a concave-down section where dead volume 435 errors become evident when the apparent Pc displacement, or the related displacement 436 value in the J-function, is noted at a wetting phase saturation below 1. Figure 6 highlights 437 this dead volume error in a dataset. Between wetting phase saturations of 1 and 0.97, some 438 data points indicate that the non-wetting phase can more readily penetrate the rock.How- 439 ever, when the J-function value exceeds 0.04, the curve characteristics shift, making it 440 harder for the non-wetting phase to enter. At this threshold, a discontinuity or change in 441 curve shape occurs, which the Brooks and Corey model cannot capture, linking it to dead 442

419

volume errors in Pc measurements. Hence, this effect should be adjusted to avoid being 443 mistakenly interpreted as a change in rock characteristics, as illustrated in Figure 7. 444

In Pc studies, dead volume is defined as the quantity of fluid (such as mercury) that 445 is presumed to fill the core sample but is, in reality, retained within the core holder or has 446 penetrated surface vugs or irregular features. According to Shafer and Neasham (2000), 447 this adjustment is known as the closure correction. In case dead volume is identified, it is 448 essential to modify the experimental data, as it fails to reflect the genuine capillary char- 449 acteristics of the core sample. 450





These observations indicated that the Brooks & Corey model, with its single specific 452 parameter, provided a simple yet accurate representation of Pc data in unconventional 453 rocks. It's important to note that these findings were derived from core samples from ba- 454 sins in the western US, reflecting a specific range of properties. Furthermore, the findings 455 of this research indicate that to effectively characterise the behaviours of unconventional 456 tight and ultra-tight rocks, the  $\lambda$  needs to be limited to a range of 0.3 to 1.5. Previously, a 457 broader index range (from 1 to 4) was applied in the MFHW cleanup study, which re- 458 quires adjustment to align with the findings presented in the following sections. 459

#### *2.3. Development, Modifying, and Validating the Model* 461

The MFHW Model was established using ECLIPSE 100 [52] to study the cleanup op- 462 eration in multiple fractured horizontal wells. The equations and underlying physics uti-<br>463 lised in Eclipse are thoroughly explained elsewhere [52] .Seven fractures were added to 464 the 600 m long horizontal well in the new pre-fractured MFHW Model. Instead of using 465 global refinement around fractures, MFHWs were built using local grid refinement (LGR). 466 Using LGR allowed the authors to capture, with minimal CPU time increase, the impact 467 of changing flow parameters in the SRV. The model's initial pressure is  $7500$  psi, and the 468 average matrix porosity is 15%. The dimensions of the numerical models are shown in 469 Table 1. The model is shown in Figure 8. The set numbers denote the sequence in which 470 they were performed as a subset of a much larger set of simulations, not all included in 471 this article. During the post-fracturing stage of the numerical modeling, controlled bot- 472 tom-hole flowing pressure was applied to produce both gas and fracturing fluid (FF), 473 which was found to be water. As shown in Figure 8, the fracture half-length is  $90$  metres 474 as mentioned in Table 1. 475

For FF, the relevant compressibility and viscosity were calculated as 0.000005 (1/psia) 476 and 0.5 cp, respectively. In the MFHW scenario's presumed base reference sets, the FF 477 injected during the hydraulic fracturing stage was twice the volume of the fracture. It is 478 important to note that a two-day period of well shut-in applied immediately after the FF 479 injection and before the flowback production. The method of validating the amended VW 480 model and its governing equations was previously discussed [30]. To validate the MFHW 481 model, the well pressures vs production time estimated by simulation were compared to 482 what was observed in an analytical model for MFHW [29]. 483

Figure 9 compares the predicted well bottom-hole pressure (Pwf) by the simulation 484 model with the analytical model as a function of production time. The fact that the two 485 curves overlap and are stacked on top of one another supports the accuracy of the 486

460

simulation model. It should be emphasised that this study takes into account twelve per- 487 tinent variables that have an impact on the post-fracturing cleanup processes. The first 488 eight values among the twelve parameters represent the exponents and endpoints of the 489 Brooks-Corey relationship for Kr in two separate phases. 490

The matrix's Pc is influenced by Km, IFT, and  $\lambda$  (pore size distribution index). The 491 final variable is Kf .Table 2 lists the possible variation ranges of the parameters. It should 492 be noted that six of the parameters given in Table 2—namely, DP, porosity of the matrix, 493 and Swc and Sgc in both the fracture and matrix—are taken into consideration constants 494 throughout a simulation set. 495

Equations 1 and 2 depict the capillary and threshold (entry) pressure, respectively 496 [50,53]. Equations 3 and 4 establish the relationship between gas and water relative per- 497 meability, as formulated by Brooks and Corey in 1966. It is important to note that data is 498 generated using either FFS or LHS sampling techniques for each simulation set, drawing 499 from the specified parameter ranges listed in Table 2. 500

$$
\frac{Pd}{IFT} = 0.0075 \times K^{-0.5}
$$

- Interfacial tension (IFT)
- Km measured in mD

$$
\left(\frac{Pd}{Pc}\right)^{\lambda} = \frac{Sw - Swr}{1 - Swr}
$$

$$
k_{rw} = K_{\max w} \times \left(\frac{Sw - Swr}{1 - Swr - Sgr}\right)^{nw}
$$

$$
k_{rg} = K_{\text{max }g} \times \left(\frac{Sg - Sgr}{1 - Swr - Sgr}\right)^{ng}
$$

Table 3 shows various simulation sets for each DP to fully understand how pressure 501 drop (DP) affects the cleanup performance. The 12 relevant parameters in this study are 502 scaled between 0 and 1, where 0 represents the lower bound and 1 represents upper limit, 503 making the assesment of the cleanup processes via the response surface approach more 504 effective (RSM). 505

# **2.4.** The main output and RSM

Gas Production Loss (GPL), expressed as a percentage, measures the effectiveness of 508 the cleanup process. It is determined by calculating the difference in cumulative fracture 509 productions between a clean, undamaged fracture and an unclean, damaged fracture, and 510 comparing it to the cumulative fracture productions of a clean, undamaged fracture. 511

$$
GPL = 100 \times \left[ \frac{FGPI_{clean} - FGPI_{unclean}}{FGPT_{clean}} \right]
$$
  
T: Field gas cumulative production

FGPT: Field gas cumulative production

After a hydraulic fracturing operation, having a clean (undamaged) fracture is ex- 512 tremely difficult or technically impossible. In order to attain a much cleaner fracture and 513 higher productivity, the current field tactics for fracturing operations could benefit from 514 additional enhancements. This would require a comprehensive understanding of the pa- 515 rameters involved and their effects on post-fracturing activities. To facilitate comparison 516 between different instances, the response parameter of GPL should be reported in a nor- 517 malised format. The present work uses tornado charts to illustrate how the 12 previously 518 listed characteristics affect gas production loss. According to this technique, if a parameter 519 positively affects cleanup effectiveness, it reduces gas production loss (GPL) or increases 520 the total amount of gas produced while the parameter is increased. In contrast, if a param- 521 eter harms cleanup effectiveness, it will result in a GPL or less cumulative gas production 522 as its value increases. Response surface methodology is frequently used to examine how 523 sensitive several relevant parameters are to a specific major output. RSMs in statistics and 524 mathematics uncover a true relationship between multiple independent variables, such as 525  $x1, x2, x3, x4,..., xn$ , and the primary output (y or f(xi)).  $526$ 

Equation 6 defines the RSM, often the polynomial that best fits the data. 527

$$
y = a_0 + \sum_{k=1}^{n} a_k x_k + \sum_{i=1}^{n} \sum_{j=i+1}^{n} a_i a_j x_i x_j + \sum_{l=1}^{n} a_l x_l^2
$$

Equation 6 lists four distinct RSM models: 528

- LRSM (Model for Linear Response Surface) with (a0) and (akxk). 529
- If (ao) and (akxk) are taken into account in addition to ( $\text{aa}_i \times \text{a}_j$ ), then LRSM with inter- 530 action (ILRSM) will be used. 531
- A pure quadratic response surface model (PQRSM) that takes into account the quad- 532 ratic terms (ao), (a $kx$ k), and (a $kx$ <sup>2</sup>).  $^{2}$ ). 533
	- The Full Quadratic Response Surface Model (FQRSM) takes this into (a $x^2$ ).

This study determined GPL as a function of those 12 pertinent factors for the Latin 535 hypercube sampling (LHS) approach using ILRSM and FQRSM models. A Python code 536 was created to perform every simulation in a simulation set, including the pre-and post- 537 processing stages of the fracturing procedure. 538

# *2.5. The second response surtface model* 540

During the flowback, some of the injected fracture fluid (FF) returns as flowback. The 541 FF volume that returns can vary greatly depending on key parameters and the design of 542 the fracture. The FF that is produced normally includes a combination of surface-returned 543 FF, some formation brine, and a portion of the injected chemicals. Consequently, under- 544 standing the volume of produced water is critical. Managing the produced FF poses a 545 significant challenge in the development and production of unconventional gas for- 546 mations due to strict regulations concerning FF flowback, its environmental impact, and 547 limited disposal options. These factors push operators to constantly review and adjust 548 their hydraulic fracturing strategies and FF flowback management approaches. To ad- 549 dress this, a new dimensionless term, Produced Fracture Fluid (PFF), was established. The 550 influence of key parameters, similar to those affecting GPL, on PFF has been examined. 551 PFF, which serves as the second response metric, indicates the proportion of flowback 552 relative to the total injected FF during the fracturing process, determined by the following 553 equation. 554

$$
PFF = 100 \times \left[ \frac{The volume of produced FF or simply Field water production}{Total FF injected at fraction stage (FF injection stage)} \right]
$$

#### *2.6. Analysis Methodology* 555

This study examines five distinct sets of MFHWs (each set consists of 1000 simulation 556 runs). Table 3 lists each of those various sets in total. The fact that each set has a reservoir 557 with identical dimensions should be emphasised. However, each set has a different Pc 558 pertinent parameter (i.e.,  $\Lambda$ ), different pressure drawdown, matrix permeability, and FF 559 injection volume. The 12 pertinent factors are considered by the base reference set, with 560 the default ranges displayed in the table. When a parameter in Table 3 has a tick next to 561 it, the parameter's default variation range is considered; else, a new range of variation is 562 established, and the name of the new sets is determined based on the degree of dissimi- 563 larity between a range of parameter values and a the set that was selected as reference. 564

## **3. Results and Analyses** 565

The previous and updated pore size distribution ranges relevant to Pc for unconven- 566 tional formations with varying Kmr, DP, and FVR were utilized. This approach aimed to 567 assess how these parameters influence cleanup efficiency when employing unconven- 568 tional Pc. The resulting data were examined, compared, and discussed in this section 569

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539

*3.1. Unconventional capillary pressure* 571

Two sets have been implemented and analysed in this section. Set 8 base reference 572 set where the dimensions and parameters variation range were shown in Tables  $1\& 2. As$  573 mentioned previously, the MFHW is shown in Figure 8.  $574$ 



**Figure 8** The modelled MFHW 576

The updated  $\lambda$  range which corresponds to the Pc values for tight/ultra-tight formations, is also used in Set 30 (0.3< $\lambda$ < 1.5),. Importantly, all parameters and dimensions 578 align with those of set 8, apart from the revised  $\lambda$  range. A comparison was made between 579 the GPL tornado chart for set 30, featuring the new  $\lambda$  range (0.3< $\lambda$ < 1.5, Figure 10), and the 580 set 26 Base Reference set (Figure 9). The comparison showed consistent trends across both 581 charts for all key parameters. Additionally, it was noted that in set 30, with its lower  $\lambda$  582 range, Pc-related parameters, particularly  $\Lambda$ , have a greater influence on GPL. This in- $583$ creased influence is attributed to the narrower  $\lambda$  range in set 30, which enhances the im- $584$ portance of Pc values relative to set 26.  $\frac{1}{2}$  585

$$
K_m \downarrow
$$
, IFT  $\uparrow$ ,  $\lambda \downarrow$ ,  $S_w \downarrow \rightarrow P_c \uparrow$  586

The effect of fluid mobility, particularly water mobility, within the matrix is slightly 587 more pronounced in set 30 contrasted to set 26, which has lower Pc values. This difference 588 arises from the higher Pc in the matrix of set 30, which hinder fluid mobility. 589



590

The tornado chart for PFF relating to set 30, utilising the updated  $\lambda$  range of 0.3 to 1.5 591 as shown in Figure 12, was in comparison to the chart for the Set 26 Base Reference set 592 that included a modified  $\lambda$  range (Figure 11). Both charts demonstrated a consistent trend 593 across all key parameters exclusive of Kf: in Set 30, an increase in Kf led to a decrease in 594 FF production (PFF), whereas the reverse effect was observed in Set 26. A new MATLAB 595 code was developed, and water saturation (Swat) as well as values from the GRDECL file 596 in Floviz at the end of the soaking period were extracted and utilized. In Eclipse simula- 597 tion, a GRDECL file defines the grid structure and geometry, including grid dimensions, 598 coordinates, and properties. It is essential for setting up the simulation as it provides the 599 spatial framework for the reservoir model. **Example 2008** 600

To further investigate the observed shift in the Kf trend shown in the PFF tornado 601 chart for Set 30, run number 29 was chosen, where Kf was set close to its maximum value. 602 A Sw map was then created to visualize water distribution at the end of the soaking period 603 for this high-Kf scenario and to contrast it with the minimum-Kf scenario, in which Kf  $604$ was set to its lowest value. 605



Examining Figures 13, 14, and 15 highlights significant contrasts between the Max- 606 Kf and Min-Kf scenarios. In the Max-Kf scenario (Figure 13), a specific zone (Region B) 607 within the first 45 meters of the fracture's half-length from the well exhibits water satura- 608 tion levels between 30% and 70%. Conversely, in the Min-Kf scenario (Figure 14), a con- 609 siderable amount of fracturing fluid (FF) is either injected into or absorbed by the matrix, 610 resulting in water saturation levels ranging from 60% to 100% (Region A) within approx- 611 imately the initial 10 meters of the fracture near the well. This disparity occurs because, 612 during FF injection, the fluid moves significantly faster and more freely through the frac- 613 ture in the Max-Kf scenario compared to the Min-Kf case. This resulted in a more dis- 614 persed FF distribution, particularly within the matrix, in the Max-Kf scenario. Therefore, 615 in the case with Min-Kf, large volume of FF is infused or imbibed within a smallermatrix 616 distance near the fracture (around  $10 \text{ m}$ ), creating Region A, which has higher water sat- 617 uration (Sw) and lower capillary pressure (Pc). This region is more easily replicated dur- 618 ing the backflow phase than in the Max-Kf scenario. 619



Pc is plotted in Figure 15 for Sets 26 and 30 (run No: 29) with different areas indicated 620 in Figures 13 and 14. From Figure 15, it is evident that Set 30 generally displays signifi- 621 cantly higher Pc values compared to Set 26. This difference is due to the narrower  $\lambda$  range 622 in Set 30 (0.3 to 1.5) compared to Set 26 (1 to 4), leading to an increase in Pc. Additionally, 623 for Set 30, the Pc curve remains identical for both Kf-Max and Kf-Min. 624

634

640

In Region A, where water saturation ranges from 60% to 100%, the capillary pressure 625 (Pc) spans from 100 psi to 20 psi for Set 30, and from 30 psi to 20 psi for Set 26. In Region 626 B, with Sw levels between 30% and 70%, Pc fluctuates between 2100 psi and 60 psi for Set 627 30, and between 80 psi and 25 psi for Set 26. Lastly, in Region C, where water saturation 628 is between 0% and 30%, Pc decreases from infinity to 2100 psi for Set 30, and from infinity 629 to 80 psi for Set 26.  $630$ 



Figure 15 Pc along with the various regions discussed, is illustrated in Figures 14 and  $13$  633

Notably, Regions A, B, and C each exhibit distinct Pc values. Through the Flowback 635 period, a rise in FF production is noted, attributed to elevated Sw values and a reduced 636 Pc, which signifies a decrease in retained FF within the set featuring the lowest Kf. This 637 explains the negative Kf value displayed in the associated tornado chart (Figure 12). 638 Kf influences FF production in two distinct ways: 639

- 1. As the value of the Kf increases, the mobility within the fracture of the FF 641 increases during the production stage necessary for increased production of 642 the FF. 643
- 2. Higher Kf increases the FF fracture mobility during the injection phase lead- 644 ing to improved distribution of the FF and reduced Sw values in the matrix 645 and hence higher Pc values that hold additional FF during the production 646 phase hence less FF output. 647

In Set 30, the second influence of Kf was notably dominant, resulting in a shift in the 648 trend of Kf in the PFF tornado chart for this set, as shown in Figure 12. Additionally, for 649 Set 30, where the  $\lambda$  range varies from 0.3 to 1.5, the parameters related to Pc, especially  $\Lambda$ , 650 had the highest impact on GPL. This is because the  $\lambda$  range of set 27 is much narrower as 651 compared to set 26 and therefore the Pc values are much more sensitive. 652

An additional key observation in the PFF tornado charts for Sets 26 and 30 (Figures 653 12 and 13) is the inverse relationship between FF production and water mobility within 654 the matrix. This is due to the dual effects of matrix water mobility on FF production: 655

- 1. 1. Maximum Kmaxwm and minimum nwm reduces the extent of water 656 bound with the matrix and increases the mobility of FF within the matrix 657 during the period of production leading to higher production of FF. 658
- 2. 2. The maximum Kmaxwm and minimum nwm also enhance the distribu- 659 tion of FF throughout the matrix during the injection phase with better dis- 660 tribution of FF throughout the matrix, lower Sw in the matrix and thus higher 661 Pc values. These elevated Pc values keep a greater amount of FF through the 662 manufacturing process, consequently lowering FF creation. 663

As shown in Figure 16, stronger Pc values in Set 30 correspond to lower FF produc- 664 tion, consistent with the fact that higher Pc values preserve FF more effectively, reducing 665 FF flowback. Figure 17 plots GPL, PFF, and cumulative gas to water production propor- 666 tion (i.e., FGPT/FWPT) for various runs in Set 30, while Figure 18 illustrates that increased 667 FF production results in higher GPL. This aligns with previous observations in sets with 668 Kmr=1, where retained FF within the matrix corresponds with reduced GPL values. 669

Investigating these two sets with two approaches toward estimating Pc highlights 670 that employing IFT reduction chemicals will increase GPL in sets with tight sand for- 671  $mation.$  672



# *3.2. Sets featuring various Kmr, FVR, and DP configurations.* 675

Therefore, to compare the cleanup efficiency under those unconventional Pc condi- 676 tions, three additional sets were conducted with Kmr=100, significantly increased FVR, 677 and high DP. The idea was to assess the impact of the given parameters on cleanup effi- 678 cacy bearing in mind unconventional Pc. Its extension was not incorporated into the sub- 679 sequent analysis of unconventional Pc because the results obtained from the analysis of 680 the SFVW and MFVW sets indicated that extensive ST further enhances FF penetration 681 within the matrix, thus enhancing FF saturation at the same time reducing the FF flow- 682 back. That, however, appears to be applicable only to the early stages of the production 683 process. 684

# *3.3. Low Km sets with unconventional Pc* 685

This Set was implemented in order to investigate the impact of a remarkably low Km 686 scale (Kmr=100) on cleanup efficiency under rather untypical Pc conditions. The Km var- 687 iation range was cut down from  $1 \text{mD-100 mD}$  in Set 30 to a new range of 0.01mD - 1 mD 688 in this set. In the analysis of the GPL tornado charts for Set 31 as a comparison to the 689 highly compact formation with that presented in Figure 19 and the Set 30 Base Reference 690 set in Figure 11 that used a different Km range, most of the key parameters had a similar 691 trend except for the Km factor. In Set 30, change in Km was seen to change GPL, with Km 692 being significantly effective on Pc as depicted in figure 10. However, in the case of Set 31, 693 there is negative relationship between Km and GPL showing an increased value of Km 694 decreases GPL with importance of Km to mobility. This shift is attributed to the low per- 695 meability characteristic of the rock in this set which greatly limits the mobility of fluids. 696 The mobility of fluids within the matrix is more critical here than in Set 30 as previously  $697$ discussed The impact of mobility of the fluids becomes very important following the al- 698 ready high values of Pc. It can be noted in figures 18 and 20; the GPL and PFF histograms 699 of the two sets show that the degree of cleanup outcomes are almost similar, due to the 700 excessive Pc values. 701

674



When the PFF chart of ultra-tight Set 31 is compared to the chart of Set 30 Base Ref- 702 erence set, all the factors described in the tornado chart of Figure 19 except Kf are similar 703 to that of Figure 12. In Set 31 Kf primary effect is higher while in Set 30 wherein the sec- 704 ondary effect of Kf is considered. The construction of the constant of  $\frac{705}{205}$ 



Figure 20 PFF Histogram chart of the effect of tightness

A comparison of the sets of unconventional formations highlights that employing 708 IFT reduction chemicals will increase GPL in sets with tight sand formation (with Km 709 variation ranges of 1  $\mu$ D-100  $\mu$ D and 0.1  $\mu$ D-10  $\mu$ D). In contrast, employing such sub- 710 stances to decrease Pc and subsequently lessen GPL in ultratight plays (i.e., km range of 711 0.01  $\mu$ D-1  $\mu$ D) is advised. In essence, it has been established that incorporating IFT (inter- 712) facial tension) reducing agents into fracturing fluids is not advisable in tight formations 713 due to its adverse effect on gas production. However, ultratight formations benefit greatly 714 from it since it increases the gas rate. 715

# *3.4. Higher FF volume sets with unconventional Pc* 717

This Set was done to determine the effect of enhancing the FVR from 2 in Set 30 to 10 718 on cleanup efficiency under unconventional Pc condition. When comparing the GPL tor- 719 nado chart for the Set 32 with FVR=10 (Figure 21) with the Set 30 Base Reference set (Figure 720 10) which incorporates adjustments to FF injection in the injection phase, similar trends 721 were observed for all the corresponding parameters on both charts. Furthermore, the fol- 722 lowing observations were made: 723

> 1.In this set, the impact of fluid mobility within the matrix and fracture on 724 GPL was more notable related to the base reference set.  $725$

> 2.The absolute values of all 12 relevant parameters at one year of produc- 726 tion were still high; it means that the cleanup process is significantly longer (up 727 to a year) compared to the duration set by MFHW, as 30. 728

These are due to the fact that the total FF volume introduced in this set is greatly 729 larger. Figure 22 also displays that the cleanup task of the high FVR configuration takes a 730

706



longer time. From Figure 23 the PFF tornado chart considering the data in Set 32, it can be 731 observed that the initial change influenced the Kf on the FF production predominantly. 732

Figure 24 provides the histogram of the PFF for the, Set 30 (FVR=2) and Set 32 (FVR=10). 733 Notably, the cumulative frequency curves of Set 32 at the three production stages con- 734 cerns not overlay one on another, unlike the Set 30 results suggesting FF manufacturing 735 goes on until one year. 736

# *3.5. Impact of increased pressure drawdon and unconventional Pc* 737

This Set was performed to capture the effect of DP increase, with new Pc, on the 738 cleanup efficiency (DP was raised from 1000 in Set 30 to 4000 in this set). Using the GPL 739 tornado chart of the Set 33 (DP=4000, Figure 25) with the GPL tornado chart of the Set 30 740 Base Reference set (Figure 10)–all the significant parameters showed the same trend as the 741 DP was changed from the earlier value. Notably, the impact of  $\Lambda$ , IFT, and Km on cumu- 742 lative gas loss was marginally less pronounced in Set 33 compared to Set 30, due to the 743 increased viscous force , i.e., higher DP, which made it more challenging to retain FF 744 within the matrix. The influence of Kf on FF flowback was minimal given the high DP 745 applied in this set (Figure 29). 746

Figures 26 and 28 indicate that larger DP didn't expedite the cleanup process in this 747 configuration with unconventional capillary pressure model. While higher DP typically 748 enhances cleanup efficiency in the fracture and adjacent matrix, Furthermore, it raises the 749 rate of FF flowback from more away from the fracture and from inside the matrix at 750 greater depths, which is not beneficial in terms of cleanup. This amplified FF flowback is 751 illustrated in Figure 28. The balancing effect of these two opposing influences resulted in 752 nearly identical cleanup performance across both sets. 753



#### **4. Conclusions** 755

This work aims to enhance the recent comprehension of HF treatments for practical 756 field usage by building upon previous research conducted by Nasriani et al. (2018), Nasri- 757 ani and Jamiolahmady (2018a and b), and Nasriani and Jamiolahmady (2019). The present 758 study seeks to investigate the effect of unconventional Pc on the cleanup effectiveness of 759 MFHWs. For this reason, an assessment of the Pc correlations presented in the current 760 paper for tight and ultra-tight formations used the Geo2Flow software.  $761$ 

For these five sets, a new term, analogous to dimensionless GPL, was incorporated 762 to depict the influence of the relevant parameters on the FF production—an aspect critical 763 to the HF of unconventional reservoirs. Outlined below are the principal findings and 764 conclusions of this work: 765

- 1. Analyses of the Pc models, based on 200 sets of conventional and unconventional Pc 766 data, revealed that the Brooks and Corey model can be used as a simple, one-param- 767 eter Pc model that adequately describes the Pc data for nonconventional formations. 768
- 2. On this basis, this research suggests that the  $\lambda$  range should be limited to the range of 769 0.3-1.5 for a better characterisation of uncon-ventional tight and ultra-tight rocks. 770 These changes were integrated into the model to reflect the unconventional Pc in the 771 new range indicated below. The same state of the stat
- 3. As mentioned earlier, this work found a concave-down section in a few Pc curves due 773 to dead volume in Pc determination. Dead volume corrections are therefore important 774 because these errors should not be confused with changes in the in-herent properties 775 of the rock. 776
- 4. As expected, various Pc-related parameters, specifically Λ, were substantially affect- 777 ing GPL in all the sets with Pc that was adjusted for unconventional cases, incorpo- 778 rated in the sets. This can be attributed to the difference in  $\lambda$  variation range identified 779

in the unconventional Pc sets, which caused the Pc more sensitive than in the conven- 780 tional sets. 781

- 5. Kf influenced FF production in two distinct ways: 782
	- A higher Kf improved FF mobility within the fractured region during the pro- 783 duction phase, leading to increased FF production. The mass of  $784$
	- Higher values of Kf also promoted increased FF mobility within the fracture 785 region throughout the injection phase and also provided better distribution 786 of FF in the fracture, lower saturation (Sw) in the matrix phase and higher Pc 787 values. These higher Pc values maintained a greater proportion of FF during 788 production and, thus, lower FF. 789
- 6. PFF tornado charts indicated a decline in FF production as water mobility within the 790 matrix increased. This outcome is due to the dual impact of matrix water mobility on 791 FF production: 792
	- More FF is produced during the production stage when there is greater ma- 793 trix water mobility, which improves FF mobility inside the matrix. 794
	- Greater FF matrix mobility through the injection phase is a result of more 795 substantial water mobility in the matrix; this leads to more dispersed FF, 796 lower matrix Sw values, and higher Pc values. Higher Pc values produce 797 less FF because they retain more FF during backflow. 798
- 7. When the same sets were exposed to the reduced Km or increased injected FF volume 799 to FVR for the sets using unconventional Pc, the outcomes were similar to when the 800 conventional Pc was used. The primary ones are: 801
	- a. It was only after bringing down the Km range or up the FVR that the cleanup 802 was significantly hampered. **803** and the set of the set
	- b. However, in the set with  $Kmr=1$ , the  $Km$  coefficient was positive suggesting  $804$ that an increase in Km raised GPL. This suggested that the Km effect which 805 reduces the value of Pc and increases the output of FF was critical. In the set 806 with  $Kmr = 100$  the  $Km$  coefficient was negative, therefore the increase of  $Km = 807$ leads to the decline of GPL. This implied that the Km actually had a great 808 influence on the mobility of the business. The cause of this change in trend is 809 that the rock in this set is very consolidated, and thus makes matrix fluid 810 movement practically impossible. 811
	- c. These are asymptotic and numerical values illustrating the impact of fluid 812 mobility on GPL at the set with a higher FVR than at the set with lower FVR. 813
- 8. As mentioned before, the cleanup process in the Set with atypical PC was not acceler- 814 ated by the augmentation of DP. This is because, as as described earlier, while increas- 815 ing DP accelerates the cleanup in the fracture and its vicinity the matrix surrounding  $816$ the fracture and at some distance away from the fracture repairs faster and reduces 817 flowback from deeper FF zones in the matrix. These two impacts tended to cancel each 818 other out and the sets with standard and unusual Pc curves revealed cleaner output 819 with comparable efficiency. The higher viscous force leads to a higher FF flowback in 820 the relevant set, and that is why there is higher FF flowback in this current high DP 821 set with atypical Pc. But the interaction of most of the FF flow back with conventional 822 PC is found at a moderate value of DP. 823
	- i. A stronger viscous force leads to the formation of more FF flow- 824 back in the relevant set, and that is why there is more FF flowback 825 in this high DP set with executive pressure coefficient that deviates 826 from the norm. However, since conventional Pc does not have as 827 much significant Pc value as the unconventional Pc to continue to 828 keep the FF inside the matrix, most of the flowback occurs at mod- 829 erate values for DP. 830
- 9. A comparison of the sets of tight and ultratight formations highlights that employing 831 IFT reduction chemicals will increase GPL in sets with tight sand formation (with Km 832 variation ranges of 1  $\mu$ D-100  $\mu$ D and 0.1  $\mu$ D-10  $\mu$ D). In contrast, employing such 833

substances to decrease Pc and subsequently lessen GPL in ultratight plays (i.e., km 834 range of 0.01  $\mu$ D-1  $\mu$ D) is advised. To put it differently, the study has established that 835 incorporating IFT-reducing agents into fracturing fluids negatively impacts gas pro- 836 duction rates in tight formations but is highly beneficial in ultratight formations as it 837 increases production rates. 838

- The wastewater or flowback fluid that returns from the well is expected to 839 have high concentrations of naturally occurring minerals and metals that 840 have dissolved into the water from the shale and other rock formations. 841
- Additionally, a small amount of the non-hazardous chemicals injected during 842 the fracturing process and naturally occurring radioactive material (NORM) 843 may be present in the fluid. Therefore, this conclusion is environmentally sig- 844 nificant. Consequently, it is strongly advised against using IFT-reducing 845 agents in tight formations to aid the matrix in imbibing most of the FF and 846 minimising flowback. 847

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